

# Reliability assessment of brittle MEMS structures based on FE- simulation, size effect theory and probabilistic sampling

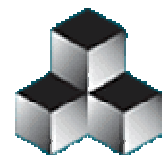
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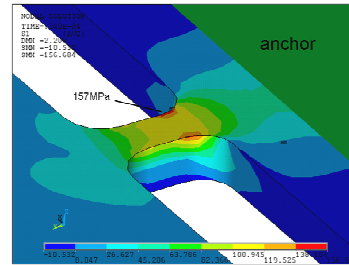
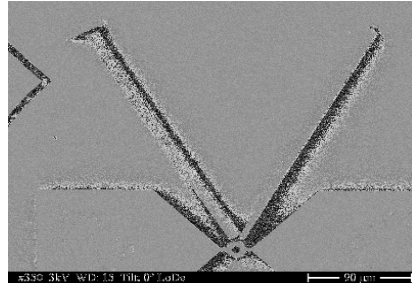
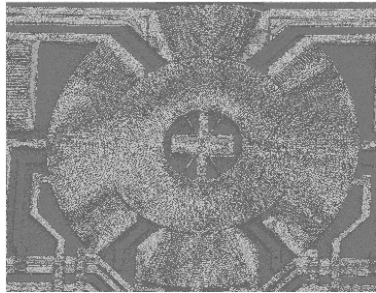


# Motivation

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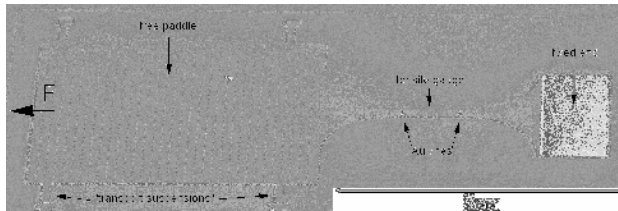
- **reliability orientated, numerical design** of brittle materials structures for microelectromechanical systems **not yet established**
- based on **Weibull parameters from tests** on „simple“ test structures and the **size effect theory** a reliability assessment for more complex structures is possible
- but **complex structures** have **deterministic parameters** in the design process
- **variances of structural parameters are not considered**
- geometrical parameters (thickness of layers, shape of cross section) material parameters (e.g. Young's Modulus) or pre-stresses (e.g. from thin layers)
- **sensitivities of structural properties** (like deformation, eigenfrequencies) in dependence of structural parameters are yet not investigated

# Procedure of design for reliability of polysilicon structures

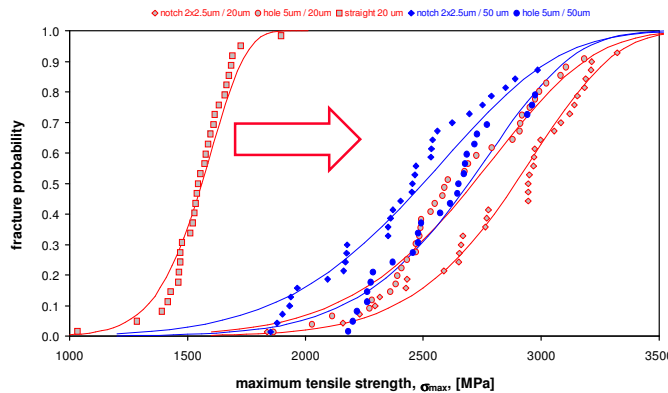
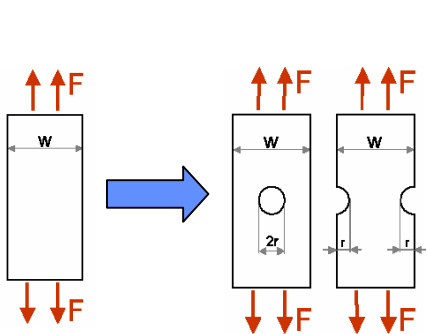


Objective: Strength and reliability assessment for load cases of complex structures **in the design or „redesign“ process**

(4) Hauck et al.

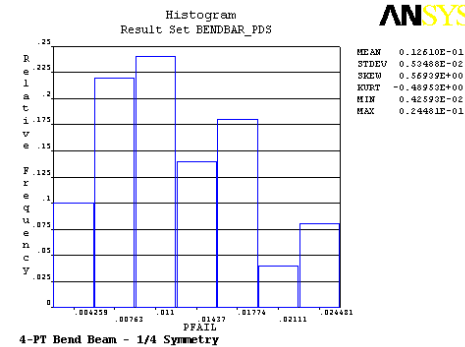


Strength test on „simple“ mechanical systems



(1) Bagdahn et al.

*Weibull- Plot of strength*

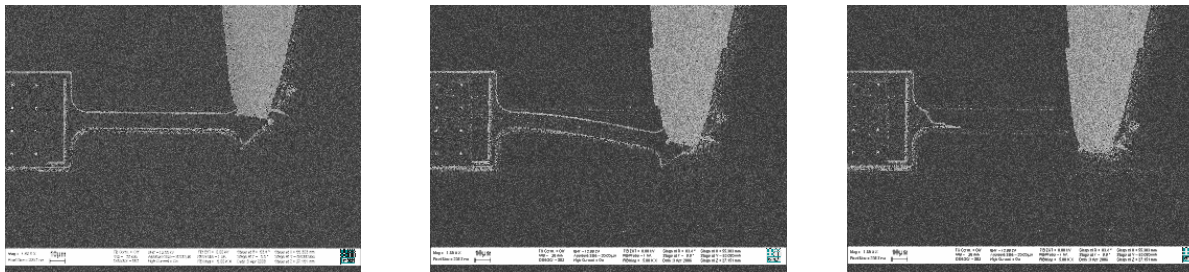
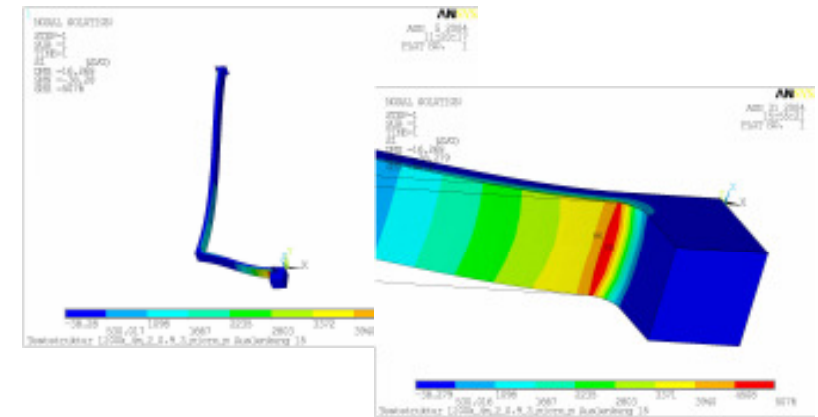


*Histogram  $p_{failure}$*

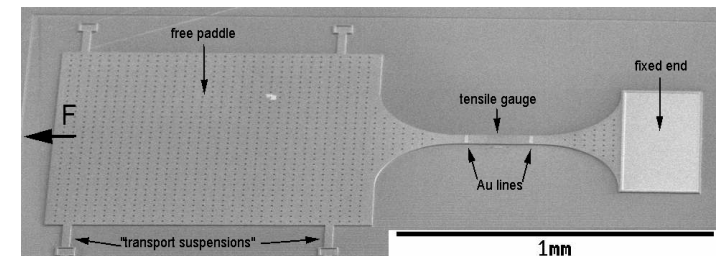
Weibull- Theory, Size effect theory and Probabilistic design

# Strength test on „simple“ mechanical systems

- probabilistic strength analysis based on the Weibull theory
- measurement of forces or displacements on test structures with simple mechanical systems
- mechanical systems: 3pb, 4pb, tensile (straight, notched, holed), also on free cut parts of the original structure
- need for numerical simulation with FE-models to get the stress values
- determination of Weibull parameters



*Bending test with FIB manipulator*

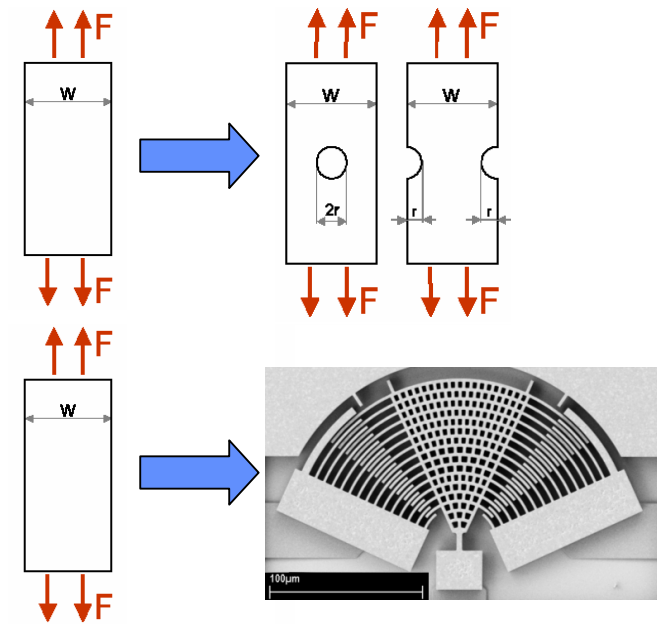


(1) Bagdahn et al.

(2) Boroch et. al.

# Size effect theory and Probabilistic design

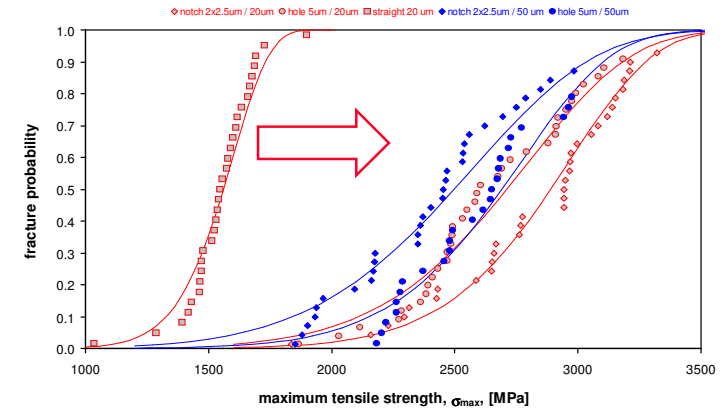
- strength assessment of complex components in design or redesign based on size effect theory of the described tests
- using Cares/Life software: time (in)dependent reliability of brittle structures, originally from NASA
- different theories to calculate effective units and scale parameters ( based on FE- models)
- reliability calculation with ANSYS PDS and Cares/Life



## Size effect

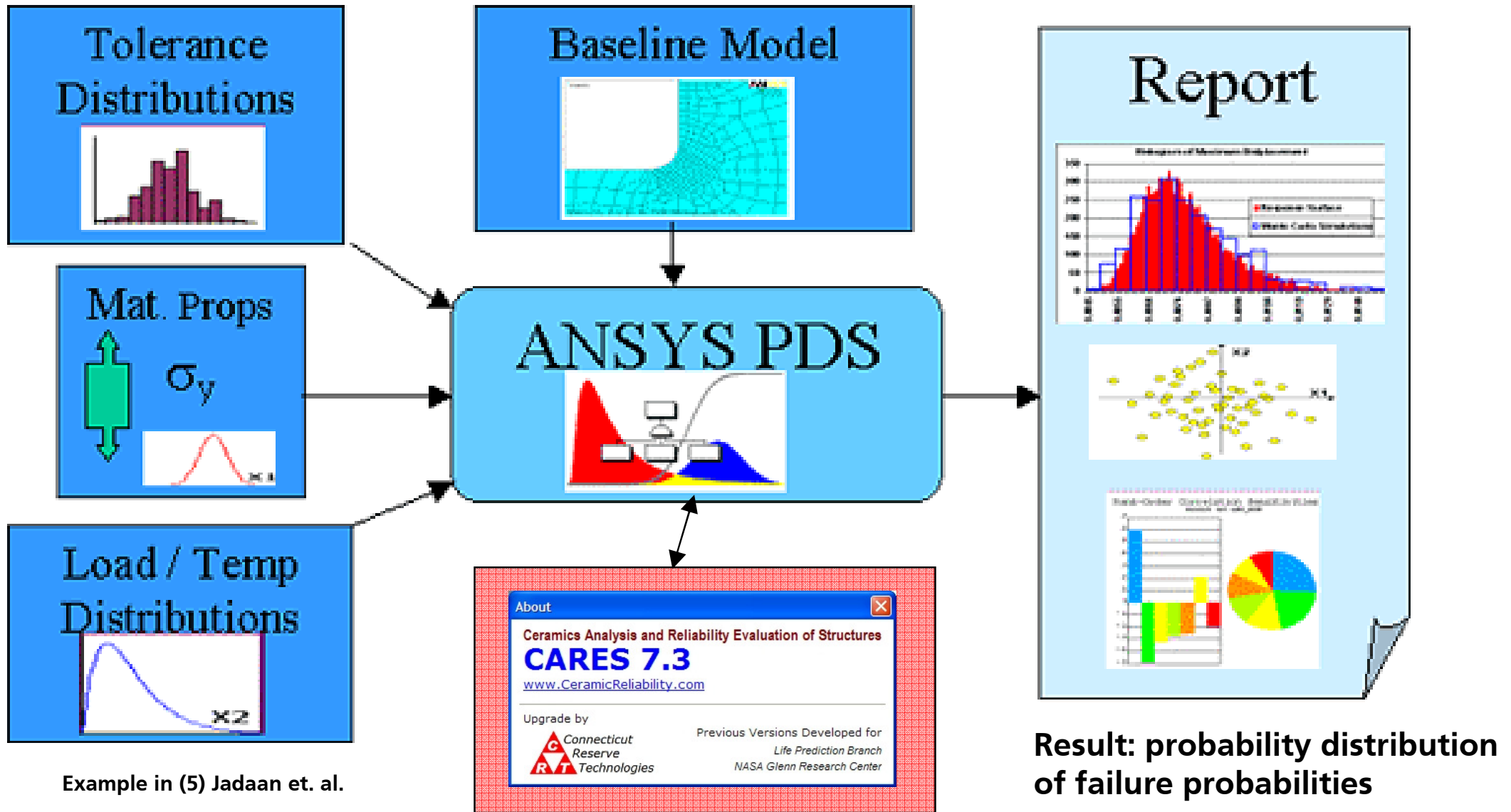
$$\sigma_{\theta c} = (1/V_e)^{1/m} \sigma_{0v} \quad \text{or} \quad \sigma_{\theta c} = (1/A_e)^{1/m} \sigma_{0A}$$

$V_e$  or  $A_e$  are the effective volume or area,  
 $\sigma_{0A}$  or  $\sigma_{0v}$  are the scale parameters  
 ("material-process" parameter)



(1) Bagdahn et al.

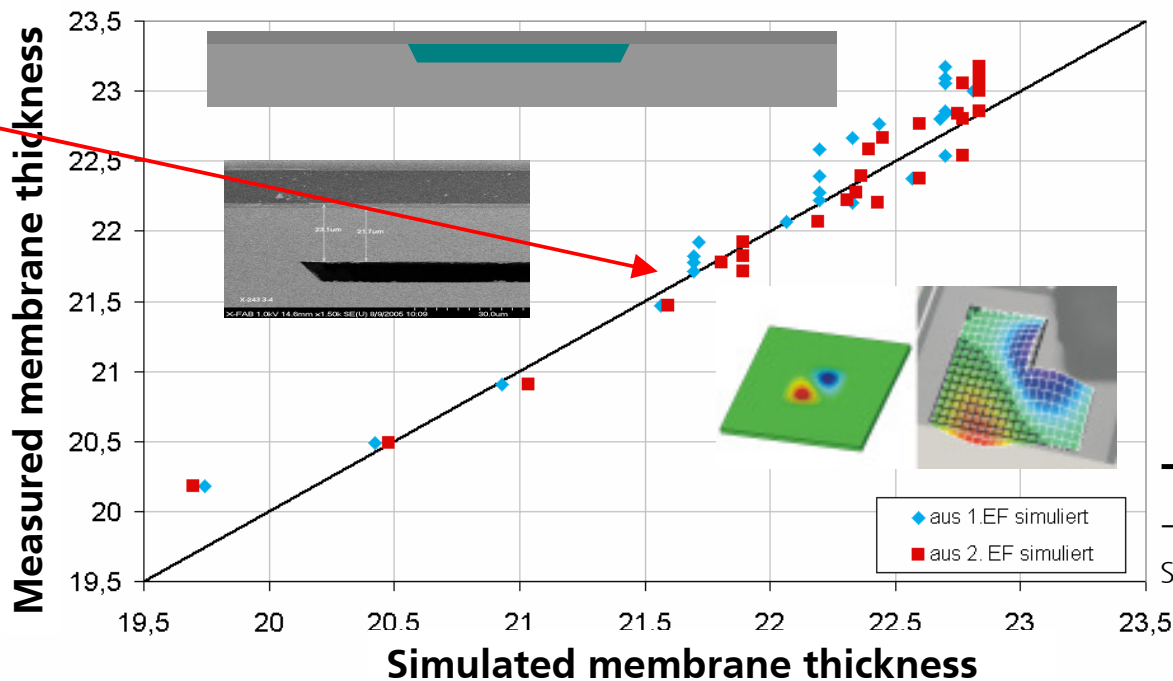
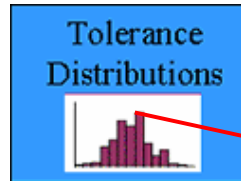
# ANSYS Probabilistic Design System- PDS



# A way to get parameter distributions

## Dynamic Characterisation of silicon MEMS

### Example: Parameter identification of 25 silicon membranes



- Polytec MSA 400 with SUSS Prober  
- at the institute since 10/2006

Source: Polytec

(3) Ebert et. al.

- important influence of the used "known" parameters for the reliability investigations
- new methods in development to characterize MEMS parameters (such pre-stress, pre-deformation, material, geometry)

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## Some literature to the topic

- (1) J. Bagdahn, W. N. Sharpe, Jr., and O. Jadaan, **Fracture strength of polysilicon at stress concentrations**, *Journal of Microelectromechanical Systems*, Vol. 12, No. 3, 2003, 302-312.
- (2) R. Borocho, J. Wiaranowski, R. Mueller-Fiedler, M. Ebert, J. Bagdahn (2007) **Characterization of strength properties of thin polycrystalline silicon films for MEMS applications**, *Fatigue & Fracture of Engineering Materials and Structures* 30 (1), 2–12.
- (3) Ebert, M.; Gerbach, R.; Bagdahn, J.; Michael, S.; Hering, S.: **Numerical identification of geometric parameters from dynamic measurement of grinded membranes on wafer level**, in Proceedings of 7th International Conference on Thermal, Mechanical and Multi-Physics Simulation and Experiments in Micro- Electronics and Micro- Systems (*EuroSimE*), L.J. Ernst et al. (Eds.), Como, Italy (2006) 208-213
- (4) Hauck, T.; Li, G.; McNeill, A.; Knoll, H.; Ebert, M.; Bagdahn, J.: **Drop simulation and stress analysis of MEMS devices**, in Proceedings of 7th International Conference on Thermal, Mechanical and Multi-Physics Simulation and Experiments in Micro-Electronics and Micro- Systems (*EuroSimE*), L.J. Ernst et al. (Eds.), Como, Italy (2006) 203-207
- (5) Jadaan et al.: „**Reliability of high temperature lightweight valve train components in a total probabilistic design environment**“, Proceeding of the 30th International **Conference on Advanced Ceramics and Composites**, Developments in Advanced Ceramics and Composites, USA, 2006